

**Errata for Book *Operations Research Models and Methods***  
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Corrections marked with a (1) superscript were added to the text after the first printing. Other corrections have not been made. Please send corrections or suggestions to one of the authors with addresses at <http://www.me.utexas.edu/~jensen/ORMM/>. Updated versions of the errata are maintained on the web site.

## **Chapter 2**

Page 43, car rental problem. Change first sentence in **Solution** section to: “The solution, whose corresponding objective function value is  $z^* = 2150$ , is shown...”

Table 2.15. The Name of Variable Number 8 should be: MTuW.

Page 45, Solution section. Change first sentence to: “The variable ... provides the solution, whose corresponding objective function value is  $z^* = 866,050$ .”

Page 50, paragraph 3, line 3. Change to: “... one column per variable (the columns for  $P_A$ ,  $P_B$ , and  $P_C$  are omitted).”

Ex. 15. The solution to the LP is not integer. There is no guarantee of integrality when the series of 1’s in each column of the LP is broken by 0’s. An integer solution is obtained by requiring the Solver to give integer answers. This makes the model into an integer program.

On page 36 in 3<sup>rd</sup> paragraph change “hours” to “minutes”.

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## **Chapter 3**

Page 61 in the last line should be “ $m$ -dimensional null vector” instead of “ $k$ -dimensional null vector”

Page 77 in the last of tables 3.6 (at the bottom of the page). Both instances of “-0.5” in the  $x_4$  column should be positive.

Page 79, Table 3.7. The last basic variable should be  $x_5$  not  $x_1$ .

Page 81, Table 3.11. The entry for  $x_3$  in row 2 should be 0 rather than 1.

Page 82, In the middle of the page the reference to Definition 4 should be to Definition 5.

Page 83, Table 3.12. The row for  $x_5$  (row 3) should be “0 1 0 0 0 1” rather than “1 0 0 0 1 1”

Page 83, Table 3.14. The circle should be around the 0.25 in the  $x_3$  column and the arrow should be pointing at the  $x_3$  column not the  $x_4$  column.

Page 83, Table 3.15.  $x_I$  should be  $x_3$ .

Page 87. The model at the bottom should be

$$\begin{aligned} &\text{Minimize } \hat{w} = \sum_{i \in F} \alpha_i \\ &\text{subject to } \sum_{j=1}^n a_{ij}x_j + \alpha_i = b_i, \quad i = 1, \dots, m \\ & \quad \quad \quad x_j \geq 0, j = 1, \dots, n; \quad \alpha_i \geq 0, i = 1, \dots, m \end{aligned}$$

Pages 87 and 88. Replace the last sentence on page 87 starting with “Stop and indicate ...” through the first paragraph on page 88 with

“Accordingly, the original problem is infeasible so the computations should be halted. The alternative situation indicates that a BFS has been found. At this point, all nonbasic artificial variables can be deleted along with all original problem variables  $x_j$  whose final phase 1 reduced costs are positive. This follows because there is no feasible solution to the original problem when any of these variables are positive. By implication then, only original problem variables with phase 1 reduced costs equal to zero need be considered in phase 2.

If some artificial variables remain in the basis at a zero level, however, then one of the following two situations arise.

(i) When one or more entries in the corresponding row are nonzero (not counting the “1” in the artificial column), the artificial variable can be left in the problem until it is replaced by some original problem variable during phase 2. The value of all basic artificial variables will remain at zero in all phase 2 solutions.

(ii) If all the entries in the corresponding row are zero except for a single “1” in the artificial column, then that row corresponds to a redundant equation in the original model. All such rows and the associated artificial columns can be deleted from the tableau before entering phase 2.”

Page 88. Replace the first sentence after the heading **Phase 2** with

“Delete the nonbasic artificial variables and any original problem variables with positive phase 1 reduced costs from the model and revert to the original objective function”

Page 88 in Phase 1 of the Example, write as

$$\begin{aligned} \text{Phase 1: } &\text{Minimize } w = && + \alpha_1 + \alpha_2 \\ &(\text{or } \text{Maximize } \hat{w} = && - \alpha_1 - \alpha_2) \\ \text{Phase 2: } &\text{Maximize } z = && -7x_1 + 3x_2 \end{aligned}$$

Page 89, Table 3.22, the 0' row is not correct. The coefficients should be 7 and  $-3$  rather than the other way.

Page 92, Table 3.25. In the Basic column, it should be  $x_4$  and  $x_5$ , not  $x_1$  and  $x_2$ .

Page 94, Table 3.30. The last entry in row 0 should be 46 (not 55).

On page 100 (last line) and 102, the table reference should be to Table 3.35 not Table 3.24.

Page 104, Exercise 5. Replace parts (b), (c) and (d) with

- (b) Using elementary row operations put the tableau in the simplex form by making  $x_1$  and  $x_4$  basic. What is the value of all variables in the new tableau.
- (c) From the new tableau predict the effects of increasing  $x_5$  by 0.5, by 1 and by 2 on  $z$ ,  $x_1$  and  $x_4$ . Note that feasibility should be maintained after  $x_5$  is increased.
- (d) From the new tableau predict the effects of increasing  $x_3$  by 0.5, by 1 and by 2 on  $z$ ,  $x_1$  and  $x_4$ . Note that feasibility should be maintained after  $x_5$  is increased.

Page 106, Exercise 20: should be  $x_j \geq 0$ , not  $0 \leq x_j \leq 1$ .<sup>1</sup>

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## Chapter 4

Page 125, Table 4.6. Bases 2, 3, 4, and 5 have typos:

- #2 should be  $x_1, x_{s2}, x_{s3}$  not  $x_{s1}, x_{s2}, x_{s3}$ ;
- #3 should be  $x_2, x_{s2}, x_{s3}$  not  $x_{s2}, x_{s2}, x_{s3}$ ;
- #4 should be  $x_1, x_{s1}, x_{s3}$  not  $x_{s1}, x_{s1}, x_{s3}$ ;
- #5 should be  $x_{s1}, x_2, x_{s3}$  not  $x_{s1}, x_{s2}, x_{s3}$ .

Exercise 11. The column in the tableau for  $x_4$  should be 0,0,1, rather than 0,1,0.<sup>1</sup>

Exercise 13(g). Change 4<sup>th</sup> to 3<sup>rd</sup>

Exercise 13(k). Say that  $x_3$  has an upper bound of 1.5 and  $x_3 = 1.5$ . The problem is ...<sup>1</sup>

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## Chapter 5

Exercise 3. In constructing the network, create a combined super source and super sink node for all external flows. Call it node 0. Arcs originating at node 0 and terminating at the plant will then represent production, while arcs leaving the outlets and terminating at node 0 will represent sales. Appropriate capacities (upper bounds) should be placed on all such arcs.

Also, the first three column headings in the table should be as follows.

Period	Manufacturing data	
	Item cost (\$)	Capacity (units)
1	\$8	175
2	10	200
3	11	150

Page 168, line 4. Should be  $x_2^* = 2.7273$ .

Exercise 10, page 177. Replace with the following.

You have two options for providing yourself with the use of a new Honda:

- A. You can purchase a contract for \$100,000 that provides you with the car for 10 years. There are no other costs associated with this option. For purposes of analysis, assume that the same contract will be available 10 years from now, and forever after.
- B. You can purchase the Honda for \$20,000 and keep it for either 2 years, 4 years or 6 years. The annual maintenance and salvage values are listed below. Resale values for odd years are not shown because they are not included as options. Again it is assumed that this or similar car will be available forever.

Year of ownership	Operating cost during year	Salvage value at year end
1	\$500	—
2	500	\$10,000
3	1000	—
4	2000	6000
5	3000	—
6	5000	2000

Maintenance and salvage values occur at the end of the year. Purchase costs are at the beginning of the year. The selection depends on your minimum acceptable rate of return, which is 25% per year. The objective is to minimize the present worth of the cost of ownership for an infinite time period.

- a. Provide a single network diagram of the problem that includes both options A and B (see machine replacement example in the text to help with the construction of the network).

b. Solve the problem and indicate the optimal resale time.

Exercise 14, page 178. Change last sentence to “Provide a node-arc structure that can be used to represent this revenue function for a minimum cost network flow programming model.”

Exercise 15. Change the last sentence to “Provide a network diagram that represents the facility.”

Exercise 16. Add the sentence “Provide a network diagram of the problem.”

Exercise 17. Change the last sentence to “Provide a network diagram of the problem and solve.”

Exercise 18. At the end of parts (a) and (b) in the problem statement, add the sentence “Provide a network diagram for this part of problem.”

Exercise 19. Add the sentence “Provide a network diagram of the problem.”

Exercise 20. Change the last sentence to “Provide a network diagram for the problem and find the optimal solution.”

Exercise 21. After the last sentence but before the *Hint*, add the sentence “Provide a network diagram for the problem.”

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## Chapter 6

Page 210, top of the page  $\pi_4$  should equal 28 not 27.

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## Chapter 7

Page 247. In demand constraint for Days-Off Scheduling problem, the index range should be  $i = 1, \dots, 7$

Exercise 1, page 255. Rephrase parts (b) and (c) as follows.

(b) Rewrite the model in part (a) as a minimization problem with all “less than or equal to” constraints.

(c) Rewrite the model in part (b) as a minimization problem with all positive objective function coefficients while keeping the variables nonnegative.

Exercise 11(a), page 258. In definition of  $x_{ij}$ , change to “... covers the demand for the next  $j$  months”

Exercise 11(b), page 259. Change the inventory variable from  $z_j$  to  $I_j$ . Also, change the instructions to “Give an MILP formulation for the problem using the new notation.”

Exercise 21(a), page 264. Should be “... shortest path tree problem ...”

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## Chapter 8

Page 299. In Step 3 of the algorithm, Equation 14 should be Equation 13.

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## Chapter 9

Page 321. Change Definition 3 to:

**Definition 3:** A function  $f(\mathbf{x})$  is convex on the convex set  $S \subseteq \mathcal{R}^n$  if and only if

$$f(\lambda \mathbf{x}_1 + (1-\lambda)\mathbf{x}_2) \leq \lambda f(\mathbf{x}_1) + (1-\lambda)f(\mathbf{x}_2)$$

for all  $\mathbf{x}_1, \mathbf{x}_2 \in S$  and for all  $0 < \lambda < 1$ . It is *strictly convex* if the inequality sign  $\leq$  is replaced with the sign  $<$ .

Page 322. Change *any* to *every* in Definition 5

Page 326. The constraints in the set  $S$  are not separated. The set should be

$$S = \{(x_1, x_2) : (0.5x_1 - 0.6)x_2 \leq 1, 2x_1^2 + 3x_2^2 \geq 27; x_1, x_2 \geq 0\}$$

Page 327. Change solution: If the equality constraint is removed the solution becomes  $\mathbf{x}^* = (2, \sqrt{2})$  with  $f(\mathbf{x}^*) = 0.586$ .

Page 335, Figure 9.13. The coordinates of the center point should be (3, 2.115).

Page 354, Exercise 16. In the equation for  $C_i(x_i)$ , it should be “for  $i = 1, \dots, 6$ ”

**Definition 5:** A set  $S \subseteq \mathcal{R}^n$  is convex if every point...

Page 340, middle of page. Replace the sentences starting with the one that begins with “The arc from ...” with:

“The arc from node 2 to node 3 allows flow from station B to station E. A nonlinear cost function of the type given in Equation (6) is associated with each station arc. For example, the flow through the arc from node 1 to node 2 is the flow rate entering station B,  $f_B$ , where  $f_B \equiv \lambda_B$ . The cost measure is the average number of units at that station, which can be written as  $L_B = f_B / (3 - f_B)$ .”

Page 348: In the table in the array describing geometric programming, the word polynomial should be polysynomial both with respect to  $f(\mathbf{x})$  and  $g_i(\mathbf{x})$

Page 349: posinomial should be spelled posynomial

Exercise 3(a), page 351: last term should be  $x_2^2$

Exercise 9(f): In second summation, change  $c(x_j)$  to  $c_j(x_j)$

Exercise 11, page 353; rephrase: “Use the definition of convexity and induction to prove Lemma 1.”<sup>1</sup>

Exercise 14, page 353; should read

“Following the suggestions in Section 9.3, prove that  $f(\mathbf{x})$  is convex if and only if

$$f(\mathbf{x}_1) \geq f(\mathbf{x}_2) + \nabla^T f(\mathbf{x}_2)(\mathbf{x}_1 - \mathbf{x}_2) \text{ for all } \mathbf{x}_1, \mathbf{x}_2 \in S$$

where  $S$  is a convex set.”<sup>1</sup>

Exercise 16. Replace with the following.

You are in charge of providing labor for a manufacturing shop for the next 6 months. Currently, there are 20 employees in the shop. Each worker costs \$1000 per month and can manufacture five units of product during the month. The cost of hiring and training a new worker is \$500. The cost of laying off a worker is \$1000. At the end of the 6-month period you want 20 persons working in the shop. All products must be sold in the month they are produced.

Demand in each month is a random variable uniform distributed over the ranges specified in the table below. If demand is lower than production capacity, some workers will be idle. If demand is higher than capacity, sales are lost with a penalty of \$200 per item not sold. To compute the expected cost of lost sales, consider month  $i$  with minimum demand  $a_i$  and maximum demand  $b_i$ . Say  $x_i$  is the capacity for production in month  $t$ . Then the expected cost of lost sales is

$$C_t(x_t) = \begin{cases} 200(b_t - a_t)/2 + 200(a_t - x_t), & \text{for } 0 \leq x_t \leq a_t \\ \frac{200}{2(b_t - a_t)}(b_t - x_t)^2, & \text{for } a_t \leq x_t \leq b_t \\ 0, & \text{for } b_t \leq x_t \end{cases} \quad t = 1, \dots, 6$$

Set up and solve the NLP to determine how many workers to hire or lay off at the beginning of each month so that the expected cost of lost sales plus the cost of providing the workforce is minimized. Workers may also be laid off at the end of month 6. Assume that sufficient capacity is provided to meet the minimum demand.

Month, $t$	Minimum demand, $a_t$	Maximum demand, $b_t$
1	50	150
2	100	200
3	75	175
4	50	150
5	200	250
6	100	200

Note that the above expression for  $C_t(x_t)$  is a piecewise nonlinear function and does not lend itself to an NLP model in continuous variables. Also, it would be better to define capacity in terms of the number of employees. This can be done by letting  $5w_t = x_t$ , where  $w_t$  is the size of the workforce in month  $t$ . Next you should derive a continuous expression for the expected cost of lost sales in terms of  $w_t$  for the case where  $5w_t \leq b_t$ ,  $t = 1, \dots, 6$ . Because the expression that you derive will not be valid when  $5w_t > b_t$ , it will be necessary to break  $w_t$  into two variables,  $u_t$  and  $v_t$ , where  $u_t$  is the number in the workforce who are idle (i.e., not producing because there is no demand) and  $v_t$  is the number in the workforce who are contributing to production.

Exercise 20, page 356; Add the following at the after the values of  $\mu$ .

Note that from Little's law discussed in Chapter 16, the average time in the system is equal to the average number in system / entering flow rate, where the entering flow rate here is equal to 0.5/min. Therefore minimizing the average time in the system when the entering flow rate is constant is equivalent to minimizing the sum of the average number at each station.

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## Chapter 10

Page 403; missing parenthesis in equation. Should be

$$f(\mathbf{x}) \cong q(\mathbf{x}) = \dots$$


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## Chapter 11

Page 423, Exercise 11: Replace parts (a) and (b) with:

- (a) Whenever a tire fails it is sent to the shop, repaired, and returned to the truck. The truck continues to operate as long as it has four good tires; otherwise, it must wait until a repaired tire is returned.
  - (b) When both spares fail, they are sent to the shop, repaired one at a time, and individually returned to the truck. The truck continues to operate as long as four good tires are available; otherwise, it must wait until a repaired tire is returned. (*Hint*: the state vector should have two components.)
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## Chapter 12

Page 429, Computer Repair example, paragraph 2, sentence 2; change to:

“Computers that fail during the day are picked up the next morning, repaired, and then returned to the office the following morning.”

Page 432, definition of  $s_2$  at bottom should be:

$s_2$  = status of the second machine (working or failed)

Page 433, line 2. Add the following sentence after the first sentence:

“For  $s_2$ , we assign a value of 0 if the second machine has not failed and a value of 1 if it has.”

Page 433, line 8, change from

"One failure leads to (1,0) and two failures lead to (2,0) ..."

to

"One failure leads to (1,0) and two failures lead to (1,1) ..."

Page 433. In Table 12.3, change the following state definitions:

$s^1 = (1,0)$ : One machine has failed and will be in the first day of repair today.

$s^2 = (2, 0)$ : One machine has failed and will be the second day of repair today.

$s^3 = (1,1)$ : Both machines have failed, one will be in the first day of repair today and the other is waiting.

$s^4 = (2,1)$ : Both machines have failed, one will be in the second day of repair today and the other is waiting.

Page 439. In matrix equation for  $\mathbf{q}$  after 2 transitions, should be:  $\mathbf{q}(2) = \dots$

Page 457, Exercise 1. Update the text as follows:

“... Assume that the order is placed just after taking inventory at the end of the week. Cars on order arrive just before inventory is taken so at that time there is always at least one car on the lot.”

Page 459, Exercise 12. Change problem statement as follows.

“Consider a process in which a single worker must perform five stages of a manufacturing process, as indicated in the figure below. For purposes of analysis, divide time into one-hour segments. When the worker is idle raw material enters the system during the next hour with probability  $p_A$ . At stage  $i$ , the probability of completing the corresponding tasks and moving on to stage  $i + 1$  during the current hour is  $p_{C(i)}$ ,  $i = 1, \dots, 5$ . Assume that no more than one stage can be completed in an hour.”

Page 460. Exercise 16. Hint: For part (c), you must consider two states when there are  $k$  printers in the shop,  $k = 1, 2, 3$ . The first is associated with the repair work that is just starting; call it *repair k\_start*. The second is associated with the repair work about to finish; call it *repair k\_finish*.

Page 463. Exercise 26 is meaningless as written. It should be replaced with the following.  
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26. Heart patients at a local hospital can be found in one of two places: the coronary care unit or in a regular room.
- If we assume that the number of heart patients remains constant and that the 1-day transition probabilities are as shown, what are the steady-state probabilities for an individual patient?

One-day transition probabilities — heart patients

	CCU	Hospital rehabilitation	Not hospitalized
Coronary care unit (CCU)	0.700	0.200	0.100
Hospital rehabilitation	0.050	0.800	0.150
Not hospitalized	0.015	0.005	0.980

- Assume persons leaving the hospital from the CCU actually die. For each fatality, a new heart patient enters a competing hospital. There is a 1-day probability of 0.05 that a patient leaves the competing hospital and enters the CCU. How would you change the 1-day transition matrix? Compute steady-state probabilities.

Page 464, Exercise 29. In table, letter “*n*” should be italic only, not bold. <sup>1</sup>

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## Chapter 13

Exercise 10(e). The expected cost vector should be:  $\mathbf{C} = (1250, 1400, 900, 0)^T$ .<sup>1</sup>

Exercise 12(a). Add to the problem statement of part a:  
“The stock price is currently \$39.”<sup>1</sup>

Exercise 13. Labels on parts d and c are switched.<sup>1</sup>

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## Chapter 14

Page 501. Second  $\mathbf{P}$  matrix is better written as:

$$= \begin{bmatrix} 1-\Delta 2 & \Delta 2 & 0 & 0 & 0 & 0 \\ \Delta 2.5 & 1-\Delta 4.5 & \Delta 2 & 0 & 0 & 0 \\ 0 & \Delta 2.5 & 1-\Delta 4.5 & 2\Delta & 0 & 0 \\ 0 & 0 & \Delta 2.5 & 1-\Delta 4.5 & \Delta 2 & 0 \\ 0 & 0 & 0 & \Delta 2.5 & 1-\Delta 4.5 & \Delta 2 \\ 0 & 0 & 0 & 0 & \Delta 2.5 & 1-\Delta 2.5 \end{bmatrix}$$

Page 503. The proportion of customers who wait; should be:  $1 - \pi_0^P - \pi_5^P$  (note error is subscript “5”).

Page 504: First heading should be: **Adding ATMs**

Page 506. Paragraph before rate matrix. Should be:  $\mu_1 = 1$  and  $\mu_2 = 2.5$ .

Should be: matrix element  $r_{43} = \mu_1 + \mu_2 = 1 + 2.5 = 3.5$ .

Page 510. It might be better to replace Table 14.5 with

Table 14.5 Probability of Completing a Specific Number of Units

Completed units, $k$	10	9	8	7	6	5	4	$\leq 3$
Probability, $p_{10-k}(14)$	0.891	0.047	0.03	0.017	0.009	0.004	0.001	0.0005

Table 14.6 (Similar change should be made.

Second row of table should be  $p_k(14)$ .

Table 14.6 Updated Probability of Completing a Specific Number of Units

Completed units, $k$	10	9	8	7	6	5	4	$\leq 3$
Probability, $p_{10-k}(14)$	0.681	0.104	0.084	0.06	0.037	0.02	0.009	0.0042

Page 516, Table 14.9. In summation term, index “ $K$ ” on  $\pi$  should be lower case. <sup>1</sup>

Page 518. Replace last sentence in last paragraph of Section **Transition Probabilities** with:

If event  $x$  occurs with rate  $\gamma_x$ , then the rate assigned to the transition would be

$$r_{ij} = \gamma_x p(i, j | x)$$

Page 521. Exercises Section. Should say “Use the Markov Analysis Excel add-in...”

Exercise 1: Rephrase and convert to five parts:

Consider Omar’s barbershop described in the previous chapter with one chair for cutting hair and three for waiting (four chairs in all). Assume that the mean time between customer arrivals is 15 minutes and the mean time for a haircut is 12 minutes. Also assume that both times are exponentially distributed and customers who arrive and find the shop full balk. In answering the following questions, provide the rate matrix and economics matrix in addition to the information requested.

- If each customer pays \$10 for a haircut use the steady-state probabilities to compute Omar’s earnings in an eight-hour day.

Now make the following changes and compute Omar’s average earnings. The changes are not cumulative.

- Add a fourth waiting chair and recomputed Omar’s earnings.
- Change one of the waiting chairs to a barber’s chair and add another barber. Omar earns \$5 for each hair cut the second barber does. When both barbers are idle, an arrival goes to Omar.
- When two or more of the waiting chairs are full Omar works faster and reduces his average cut time to 10 minutes.
- Change the arrival process. When all the waiting chairs are empty, all the arrivals enter. When one waiting chair is occupied, 1/3 of the arrivals balk. When two of the waiting chairs are occupied, 2/3 of the arrivals balk. When all three chairs are occupied, all the arrivals balk.

Exercise 13, part a: Restate as “Draw the rate network for the number of printers in the queue.”

Exercise 13, part c: Change to: “Find the steady-state probabilities. What is the production (completion) rate of this system with and without failures? *Hint*: A board is produced when no fault is detected during inspection or when a repair is completed. Use the Markov Analysis add-in to create a matrix under the Economics button. Place a 1 in each cell that represents a production event.”

Exercise 13: See updated solutions. The original rate matrix was not correct.

Exercise 14, parts c, d, e: The data in the tables for “Mean Time” should be shifted to the left to line up with the column headers. <sup>1</sup>

Exercise 15, parts a and b: The data in the tables for “Mean Time” should be shifted to the left to line up with the column headers. <sup>1</sup>

## Chapter 16

Page 563, in table at bottom for  $M/M/2$ , change  $\rho = \lambda/s\mu$  to  $\rho = \lambda/2\mu$ . Also, give second formula for  $L$ :

$$L = L_q + L_s = L_q + \lambda/\mu = 0.8727^1$$

The corrections for pages 563, 572 and 573 were suggested by R.G. Vickson, University of Waterloo.

Page 563. In the expression for  $\Pr\{T_{sys} > t\}$  the term in the inner parentheses becomes indeterminate when  $s-1-s\rho=0$ . To address this situation, change the sentence before the expression for  $\Pr\{T_{sys} > t\}$  to:

Without going through the details, the result for  $s-1-s\rho \neq 0$  is

$$\Pr\{T_{sys} > t\} = e^{-\mu t} \left[ 1 + \frac{(s\rho)^s \delta_0}{s!(1\rho)} \left( \frac{1e^{\mu t(s-1-s\rho)}}{s!s\rho} \right) \right], \quad t \geq 0 \text{ and } 0 < \rho < 1$$

(add the following)

When  $s-1-s\rho=0$ , a singularity occurs in the denominator of the inner term in parentheses. To analysis this case, it is more convenient to write the above expression in terms of  $\lambda$  and  $\mu$  by substituting  $\rho = \lambda/s\mu$  everywhere. Now, taking the limit of the fraction in the inner parentheses as  $\lambda \rightarrow \mu(s-1)$  gives

$$\Pr\{T_{sys} > t\} = e^{-\mu t} \left[ 1 + \frac{(\lambda/\mu)^s \pi_0}{s!(1-\lambda/s\mu)} (\mu t) \right], \quad t \geq 0 \text{ for } \frac{\lambda}{\mu} = s-1$$

where

$$\pi_0 = \left[ \sum_{n=0}^{s-1} \frac{(\lambda / \mu)^n}{n!} + \frac{(\lambda / \mu)^s}{s!(1 - \lambda / s\mu)} \right]^{-1}$$

in both equations for  $\Pr\{T_{sys} > t\}$ . Note that when taking the limit, it is necessary to use L'Hospital's rule because the fraction is 0/0 at  $s-1-s\rho=0$ .

(It may be a good idea to derive the above expression for the case where  $s-1-s\rho=0$ .)

Page 572-573. The section of Finite Input Source Systems has several errors. The last sentence of the first paragraph of the section should read.

We assume arrivals balk when  $n = K$  and  $K \leq N$ . The results of the section also hold when the maximum number in the system is equal to the population.

The expression for  $q_n$  should be:

$$q_n = \frac{(N-n)\pi_n}{N-L-(N-K)\pi_K} \text{ for } n = 0, \dots, K-1,$$

Page 573. In Figure 16.10, the expression for  $P_B$  should be:

$$P_B = \sum_{n=s}^K \pi_n$$

The expression for the average arrival rate should be

$$\bar{\lambda} = \lambda [N - L - \pi_K (N - K)] \text{ for } K \leq N$$

Page 578. In Table 16.9 for Case 3, should be:  $L_q = 5.657$

Exercise 7. Change last sentence in first paragraph to: "Assume that the system is in steady state, and in parts a - e,..."

Exercise 7. Change part (b) to:

- b. When a motorist is filling up, all other customers must wait on the street. How many spaces for cars should be made available on the station property to assure that there is sufficient room to wait there 85% of the time?

Exercise 15. Remove second occurrence of sentence "The company has two technicians who can ... to effect a repair." Also, change "affect" to "effect" in first occurrence.<sup>1</sup>

Exercise 17. Change the service rate to 8 customers per hour for a better problem.<sup>1</sup>

## Chapter 18

Exercise 4(d). Use  $t = 1$ .<sup>1</sup>

Exercise 10(b) and (c). Should ask for 12 replications rather than 10.<sup>1</sup>

Exercise 15. Add the sentence: Simulate the process of passing from system 1 to system 2 with a Bernoulli random variable.<sup>1</sup>

Exercise 21. Should refer to Table 18.19 rather than Table 18.20. Note that Table 18.19 in Chapter 18 is in error as well as Appendix A1 of the simulation chapter.<sup>1</sup>

Table 18.19 is in error. The correct table should be:<sup>1</sup>

Table 18.19 Error as Function of Sample Size for Inventory Simulation

Measures	Demand ( $D$ )	Lead time ( $T_L$ )
Estimated mean	11.65	2.8
Estimated standard deviation	2.594	0.980
Estimated size ( $n$ ) for 1% error	3290	8127
Sample size ( $n$ ) for 5% error	77	188
Sample size ( $n$ ) for 10% error	14	33

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### Supplement

The discussion concerning confidence limits in the Simulation supplement distributed on the original edition student disk is in error. It is corrected on the Teach ORMM CD and on the web. The correct confidence limit discussion is below.

#### Confidence Intervals

Once  $\bar{x}$  and the *standard error of the mean*,  $\sigma_{\bar{x}}$ , are determined, the confidence interval and maximum error for  $\mu_X$  are given by

$$\mu_x = \bar{x} + z_{\alpha/2} \sigma_{\bar{x}} \quad (\text{A.6})$$

or

$$\mu_x = \bar{x} + t_{\alpha/2} \hat{\sigma}_{\bar{x}} \quad (\text{A.7})$$

as the case may be, where  $\hat{\sigma}_{\bar{x}}$  is the estimated standard error when (A.5) is used in place of  $\sigma_{\bar{x}}^2$  in (A.3) or (A.4). For A.7, the value of  $t_{\alpha/2}$  depends on the number of degrees of freedom,  $df$ , where  $df = n - 1$ . If  $\sigma_X$  is known, then the maximum error  $\varepsilon$  for a given level of confidence can be found from

$$\varepsilon = z_{\alpha/2} \sigma_{\bar{x}} \text{ or } z_{\alpha/2} \sigma_x / \sqrt{n}$$

when (A.3) applies. It follows that

$$n = \left( \frac{z_{\alpha/2} S_x}{e} \right)^2 \tag{A.8}$$

provides the required sample size which satisfies a given maximum error and confidence level.

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### **Error in Probability Supplement**

Page 24

*The c.d.f. of the Triangular Distribution*

$$F(x) = \begin{cases} 0, & \text{for } x \leq 0 \\ \frac{x^2}{c}, & \text{for } 0 < x \leq c \\ \frac{x(2-x)-c}{(1-c)}, & \text{for } c < x < 1 \\ 1, & \text{for } x \geq 1 \end{cases} .$$